

er n, entonces la expresión del término

se puede expresar utilizando alguno o
sucesión recursiva es necesario dar a
término anterior al término general

que se define como:
una de los dos términos anteriores,

escrita por Fibonacci como la
conejos: "Cierta hombre tiene
n lugar cerrado y desea saber
este par en un año cuando,
pareja necesita un mes para
crea otra pareja"
Fibonacci's Liber Abaci, página 404)

- a) $a_n = 5^n$
- b) $a_n = (-1)^n (2n)$
- c) $a_n = 2^2 + n^2$

- d) $a_n = \frac{3n}{1+2n}$
- e) $a_n = (-1)^n (5n-3)$
- f) $a_n = n^n + n^2 + 2n + 1$

- g) $a_n = 4 + (-4)^n$
- h) $a_n = 7 + \frac{1}{3^n}$

a) $a_n = 5^n$

$5_1 = 5$

$5_2 = 25$

$5_3 = 125$

$5_4 = 625$

$5_5 = 3125$

b) $a_n = (-1)^n (2n)$

$a_1 = 2$ $a_2 = -4$ $a_3 = 6$ $a_4 = -8$

c) $a_n = 2^2 + n^2$

$a_1 = 5$ $a_2 = 8$ $a_3 = 13$ $a_4 = 20$ $a_5 = 29$ $a_6 = 40$

$a_7 = 53$ $a_8 = 72$ $a_9 = 97$ $a_{10} = 130$

d) $a_n = \frac{3n}{1+2n}$

$a_1 = 1$ $a_2 = \frac{6}{5}$ $a_3 = \frac{9}{5}$

$a_4 = \frac{12}{7}$ $a_5 = \frac{15}{7}$

e) $a_n = (-1)^n (5n-3)$

$a_1 = 2$ $a_2 = -7$ $a_3 = 12$

f) $a_n = n^n + n^2 + 2n + 1$

$a_1 = 5$ $a_2 = 15$ $a_3 = 49$

$a_4 = 281$ $a_5 = 3162$

g) $a_n = 4 + (-4)^n$

$a_1 = 0$ $a_2 = 20$ $a_3 = 60$

$a_4 = 260$ $a_5 = 1020$

h) $a_n = 7 + \frac{1}{3^n}$

$a_1 = \frac{22}{3}$ $a_2 = \frac{196}{27}$ $a_3 = \frac{1207}{243}$

$a_4 = \frac{6n}{9}$ $a_5 = \frac{368}{81}$

3 Encuentra el término indicado en cada sucesión.

a) a_n , si $a_1 = 3$ y $a_n = -2 + a_{n-1}$

b) b_n , si $b_1 = 0,25$ y $b_n = 4b_{n-1}$

c) c_n , si $c_1 = 2$ y $c_n = c_{n-1}$

d) a_n , si $a_1 = 0$, $a_2 = 1$ y $a_n = 2a_{n-1} + a_{n-2}$

a) $a_1 = 3$
 $a_2 = 1$
 $a_3 = -1$
 $a_4 = -3$

e) $c_1 = 2$
 $c_2 = 2$
 $c_3 = 2$
 $c_4 = 2$

b) $b_1 = 0,25$
 $b_2 = 1$
 $b_3 = 4$
 $b_4 = 16$
 $b_5 = 64$
 $b_6 = 256$

d) $a_3 = 2 - 1 = 1$
 $a_4 = 2 \cdot 2 + 1 = 5$
 $a_5 = 2 \cdot 5 + 2 = 12$

1 Escribe las sumas

a $4+7+10+13+16+\dots+28$ c $\frac{4}{5} + \frac{5}{6} + \frac{6}{7} + \dots + \frac{23}{24}$ e $8+15+24+35+\dots$
 b $3+3+3+3+3+3+3$ d $1 + \frac{1}{3} + \frac{1}{9} + \dots + \frac{1}{343}$ f $\frac{1}{2} + \frac{1}{6} + \frac{1}{12} + \dots$

$\sum_{k=1}^6 \frac{1}{2k} = \frac{1}{2} + \frac{1}{4} + \frac{1}{6} + \frac{1}{8} + \frac{1}{10} + \frac{1}{12}$

$\sum_{n=2}^{10} \frac{1}{n^2-1} = \frac{1}{2^2-1} + \frac{1}{3^2-1} + \frac{1}{4^2-1} + \frac{1}{5^2-1} + \frac{1}{6^2-1} + \frac{1}{7^2-1} + \frac{1}{8^2-1} + \frac{1}{9^2-1} + \frac{1}{10^2-1}$
 $= \frac{1}{3} + \frac{1}{8} + \frac{1}{15} + \frac{1}{24} + \frac{1}{35} + \frac{1}{48} + \frac{1}{63} + \frac{1}{80} + \frac{1}{99} = \frac{36}{55}$

c $\sum_{n=1}^8 (4)^{n+1} \cdot n!$
 $= (4^2 \cdot 1!) + (4^3 \cdot 2!) + (4^4 \cdot 3!) + (4^5 \cdot 4!) + (4^6 \cdot 5!) + (4^7 \cdot 6!) + (4^8 \cdot 7!) + (4^9 \cdot 8!)$
 $= (1 \times 4) + (1 \times 8) + (1 \times 16) + (1 \times 24) + (1 \times 40) + (1 \times 60) + (1 \times 84) + (1 \times 112)$
 $= 4 + 8 + 16 + 24 + 40 + 60 + 84 + 112 = 204$

d $\sum_{n=1}^5 3^n(n+1) = (3^1 \cdot 2) + (3^2 \cdot 3) + (3^3 \cdot 4) + (3^4 \cdot 5) + (3^5 \cdot 6)$
 $= 6 + 9 + 36 + 135 + 243 = 1.646$

e $\sum_{n=1}^3 \frac{3n-1}{n} = \frac{3 \cdot 1 - 1}{1} + \frac{3 \cdot 2 - 1}{2} + \frac{3 \cdot 3 - 1}{3} = 2 + \frac{5}{2} + \frac{8}{3} = 2 + 2.5 + 2.666 = 7.166$

f $\sum_{n=1}^4 \frac{1}{n} = 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} = 2.083$

g $\sum_{n=1}^4 \frac{1}{\sqrt{n}} = 1 + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{3}} + \frac{1}{\sqrt{4}} = 1 + 0.707 + 0.577 + 0.5 = 2.784$

h $\sum_{n=1}^4 (1 + \frac{1}{n}) = 4 + 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} = 5.083$

2 Encuentra el valor de cada suma

a $\sum_{k=1}^6 \frac{1}{2k}$ c $\sum_{n=1}^8 (4)^{n+1} \cdot n^2$ e $\sum_{n=1}^9 \frac{3n-1}{n}$ g $\sum_{n=1}^7 \frac{1}{\sqrt{n}}$
 b $\sum_{n=2}^{10} \frac{1}{n^2-1}$ d $\sum_{n=1}^5 3^n(n+1)$ f $\sum_{n=1}^5 \left(\frac{2}{7}\right)^{n-1}$ h $\sum_{n=1}^7 (1 + \frac{1}{n})$

$\sum_{n=1}^{10} \frac{1}{\sqrt{n}} - \frac{1}{\sqrt{n+1}} = \left(\frac{1}{\sqrt{1}} - \frac{1}{\sqrt{2}}\right) + \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{3}}\right) + \left(\frac{1}{\sqrt{3}} - \frac{1}{\sqrt{4}}\right) + \left(\frac{1}{\sqrt{4}} - \frac{1}{\sqrt{5}}\right) + \left(\frac{1}{\sqrt{5}} - \frac{1}{\sqrt{6}}\right) + \left(\frac{1}{\sqrt{6}} - \frac{1}{\sqrt{7}}\right) + \left(\frac{1}{\sqrt{7}} - \frac{1}{\sqrt{8}}\right) + \left(\frac{1}{\sqrt{8}} - \frac{1}{\sqrt{9}}\right) + \left(\frac{1}{\sqrt{9}} - \frac{1}{\sqrt{10}}\right) + \left(\frac{1}{\sqrt{10}} - \frac{1}{\sqrt{11}}\right)$
 $= 1 - \frac{1}{\sqrt{11}}$

$4 \sum_{n=1}^7 \left(1 + \frac{2}{n}\right)^n = 4 \left[\left(1 + \frac{2}{1}\right)^1 + \left(1 + \frac{2}{2}\right)^2 + \left(1 + \frac{2}{3}\right)^3 + \left(1 + \frac{2}{4}\right)^4 + \left(1 + \frac{2}{5}\right)^5 + \left(1 + \frac{2}{6}\right)^6 + \left(1 + \frac{2}{7}\right)^7 \right]$
 $= 4 \left[3 + (1+1)^2 + \left(1 + \frac{2}{3}\right)^3 + \left(1 + \frac{2}{4}\right)^4 + \left(1 + \frac{2}{5}\right)^5 + \left(1 + \frac{2}{6}\right)^6 + \left(1 + \frac{2}{7}\right)^7 \right]$
 $= 4 \left[3 + 2 + \frac{27}{8} + \frac{25}{4} + \frac{3125}{3125} + \frac{1296}{1296} + \frac{16807}{16807} \right]$
 $= 4 \left[5 + \frac{503}{70} \right] = \frac{2800 + 2012}{70} = \frac{4812}{70}$

5 Emplea not

a La sum

b La sum

3 Halla la suma de los diez primeros términos de cada una de las siguientes series:

a $a_n = 5^n - 5^{n-1}$

c $a_n = n2^{n-1}$

e $a_n = 2n(2n-1)$

b $a_n = \frac{1}{n(n+1)(n+2)}$

d $a_n = \left(\frac{1}{4}\right)^n + 3^{\frac{n}{5}}$

f $a_n = n! - (n-1)!$

A = $4 + 20 + 100 + 500 + 2.500 + 12.500 + 62.500 + 312.500 + 1.562.500 + 7.812.500 = 9.765.624$

B = $\frac{1}{6} + \frac{1}{24} + \frac{1}{60} + \frac{1}{120} \dots + \frac{1}{840} = \frac{65}{1240}$

C = $1 + 4 + 12 + 32 + 80 \dots + 5120 = 9217$

D = $\frac{1}{4} + 3\frac{1}{3} + \frac{1}{16} + 3\frac{1}{2}$

E = $2 + 12 + 30 + 56 \dots + 380 = 1430$

F = $1 + 2 + 2 + 4 + 4 \dots + 1316818944600 = 1331657196939$