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$$3) \int_2^3 x dx$$

$$= \frac{x^2}{2} \Big|_2^3 = \frac{3^2}{2} - \frac{2^2}{2} = \frac{9-4}{2} = \frac{5}{2}$$

$$= 2.5 \times 5$$

$$= 12.5$$

$$6) \int_0^6 3\sqrt{x}$$

$$= \int_0^6 x^{1/2} dx = \frac{1}{3} + 1 = \frac{1}{2} + \frac{3}{2} = \frac{4}{3}$$

$$= \int_0^6 \frac{3x^{1/2}}{\frac{2}{3}} = \int_0^6 \frac{3x^{1/2}}{4} = \frac{3\sqrt[3]{x^4}}{4}$$

$$= \int_0^6 3 \frac{\sqrt[3]{x^4}}{4} \Big|_0^6 = \frac{3\sqrt[3]{6^4}}{4} - \frac{3\sqrt[3]{0^4}}{4} = \frac{3 \cdot 11}{4} - \frac{0}{4}$$

$$= \frac{33}{4} - \frac{0}{4} = \frac{33}{4}$$

$$= 8.25$$

$$2) a) \int_1^7 6(f(x) - \frac{1}{2}g(x)) dx$$

$$= 5 \int_1^7 (f(x) dx - \frac{1}{2} \int_1^7 g(x) dx)$$

$$= 5 [3 - \frac{1}{2} (\int_1^3 g(x) dx + \int_3^7 g(x) dx)]$$

$$= 5 [3 - \frac{1}{2} (-5 - 3)]$$

$$= 5 [3 - \frac{1}{2} (-8)]$$

$$= 5 [3 + 4]$$

$$= 5 \cdot 7$$

$$= 35$$

$$6 \int_1^7 -2f(x) dx + \int_1^7 16g(x) dx$$

$$= -2 \int_1^7 f(x) dx + 6 \int_1^7 g(x) dx$$

$$= -2 \cdot 3 + 6(-8)$$

$$= -6 - 48$$

$$= -54$$

$$c) \int_0^3 (f(x) + g(x)) dx$$

$$= \int_0^3 f(x) dx + \int_0^3 g(x) dx$$

$$= 3(3) + (-8)$$

$$= 3(-5)$$

$$= 3 \cdot -5$$

$$= -15$$

$$c) \int_0^3 \frac{x}{2} dx$$

$$= \frac{x^2}{2} \Big|_0^3 = \frac{3^2}{4} - \frac{0^2}{4}$$

$$= \frac{9}{4} = 2.25$$