

$$2. a) \int_1^7 5 \left(f(x) - \frac{1}{2} g(x) \right) dx$$

$$= 5 \int_1^7 \left(f(x) - \frac{1}{2} g(x) \right) dx$$

$$= 5 \left[\int_1^7 f(x) dx - \frac{1}{2} \int_1^7 g(x) dx \right]$$

$$= 5 \left[3 - \frac{1}{2} \left(\int_1^3 g(x) dx + \int_3^7 5(x) dx \right) \right]$$

$$= 5 \left[3 - \frac{1}{2} (-5 - 3) \right]$$

$$= 5 \left[3 - \frac{1}{2} (-8) \right]$$

$$= 5 [3 + 4]$$

$$= 5 \cdot 7$$

$$= 35$$

$$b. \int_1^7 -2 f(x) dx + \int_1^7 6 g(x) dx$$

$$= -2 \int_1^7 f(x) dx + 6 \int_1^7 g(x) dx$$

$$= -2 \cdot 3 + 6(-8)$$

$$= -6 - 48$$

$$= -54$$

$$\begin{aligned}
 C \int_1^7 3(f(x) + g(x)) dx & \\
 = 3 \int_1^7 f(x) + \int_1^7 g(x) & \\
 = 3(3 + (-8)) & \\
 = 3(-5) & \\
 = 3 \cdot -5 & \\
 = -15 &
 \end{aligned}$$

$$1. f(x) = mx + b$$

$$b = 3$$

$$\begin{aligned}
 m &= \frac{y_2 - y_1}{x_2 - x_1} \\
 &= \frac{4 - 3}{7 - 0} \\
 &= \frac{1}{7}
 \end{aligned}$$

$$f(x) = x + 3$$

$$\begin{aligned}
 \int_{-3}^7 x + 3 dx &= \int_{-3}^7 x dx + \int_{-3}^7 3 dx \\
 &= \left. \frac{x^2}{2} \right|_{-3}^7 + \left. 3x \right|_{-3}^7 \\
 &= \frac{(7)^2}{2} - \frac{(-3)^2}{2} + 3(7) - 3(-3) \\
 &= \frac{49}{2} - \frac{9}{2} + 21 + 9 \\
 &= 2
 \end{aligned}$$

$$3. \\ a \int_2^3 x dx$$

$$= \frac{x^2}{2} \Big|_2^3 = \frac{3}{2} \frac{-2^2}{2} = \frac{9-4}{2} = \frac{5}{2}$$

$$= 2.5 \times 5$$

$$= 12.5$$

$$b \int_0^6 \sqrt[3]{x} dx$$

$$= \int_0^6 x^{1/3} dx = \frac{1}{\frac{1}{3} + 1} = \frac{1}{\frac{4}{3}} = \frac{3}{4}$$

$$= \int_0^6 \frac{x^{4/3}}{\frac{4}{3}} = \int_0^6 \frac{3x^{4/3}}{4} = \frac{3}{4} \sqrt[3]{x^4}$$

$$= \int_0^6 \frac{3 \sqrt[3]{x^4}}{4} \Big|_0^6 = \frac{3 \sqrt[3]{6^4}}{4} - \frac{3 \sqrt[3]{0^4}}{4} = \frac{3 \cdot 11}{4} - \frac{0}{4}$$

$$= \frac{33}{4} - \frac{0}{4} = \frac{33}{4}$$

$$= 8.25$$

$$C \int_0^3 \frac{x}{2} + 1$$

$$= \frac{x^2}{2} + x \Big|_0^3 = \frac{3^2}{2} + 3 - \frac{0^2}{2} - 0$$

$$= \frac{9}{2} + 3 = 2.25 + 3 = 5.25$$